

$0^\circ \leq \theta < 90^\circ$ のとき、次の式を計算せよ.

$$\left\{ \left(\frac{1}{\cos \theta} + \tan \theta \right)^4 + \left(\frac{1}{\cos \theta} - \tan \theta \right)^4 \right\}^2 - \left\{ \left(\frac{1}{\cos \theta} + \tan \theta \right)^4 - \left(\frac{1}{\cos \theta} - \tan \theta \right)^4 \right\}^2$$

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【答】 4

【解答】

$A^2 - B^2 = (A + B)(A - B)$ を用いて与式を変形する.

$$\begin{aligned} & \left\{ \left(\frac{1}{\cos \theta} + \tan \theta \right)^4 + \left(\frac{1}{\cos \theta} - \tan \theta \right)^4 \right\}^2 - \left\{ \left(\frac{1}{\cos \theta} + \tan \theta \right)^4 - \left(\frac{1}{\cos \theta} - \tan \theta \right)^4 \right\}^2 \\ &= 2 \left(\frac{1}{\cos \theta} + \tan \theta \right)^4 \cdot 2 \left(\frac{1}{\cos \theta} - \tan \theta \right)^4 \\ &= 4 \left(\frac{1}{\cos^2 \theta} - \tan^2 \theta \right)^4 \\ &= 4 \left(\frac{1 - \sin^2 \theta}{\cos^2 \theta} \right)^4 \\ &= 4 \end{aligned}$$

……(答)

である.